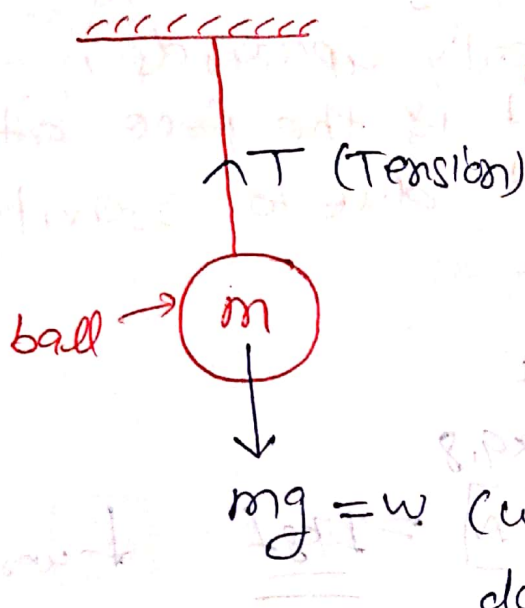


# Chapter - 1

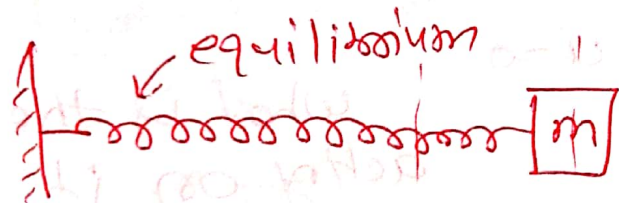
## ∴ Force ∴

Q1

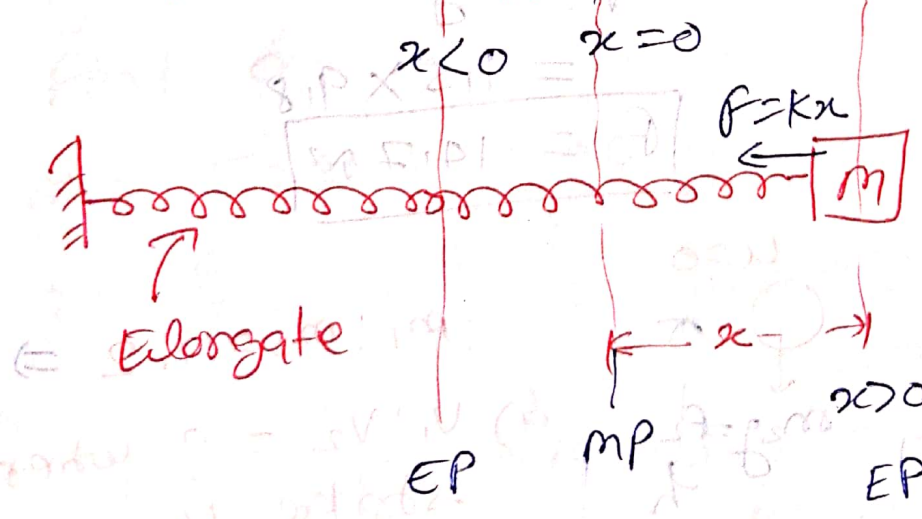
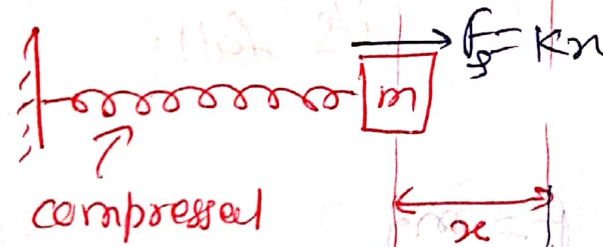


A ball is hanging, draw FBD on the ball and string

Q2

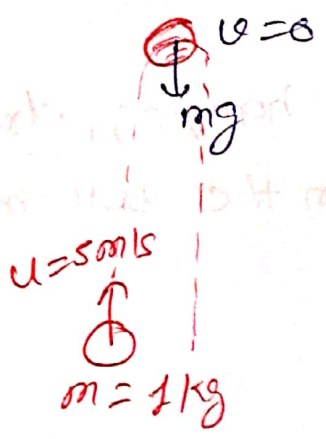


Spring force  
$$F_s = -kx$$



Numericals 1.1

①



A body of mass 1kg throw vertically upwards, what is the force at highest point due to gravity.

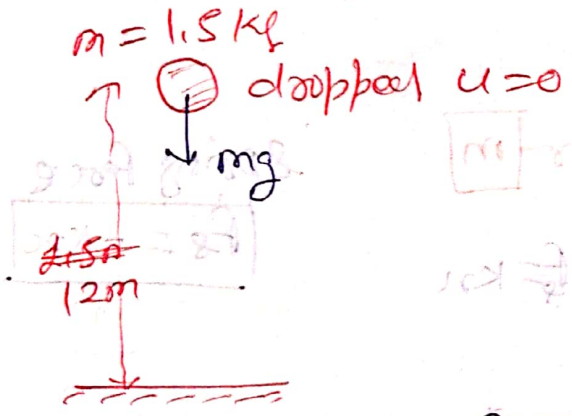
$$F = mg$$

$$= 1 \times 9.8$$

$$F = 9.8 \text{ N} = 1 \text{ kgf}$$

↓ words.

②



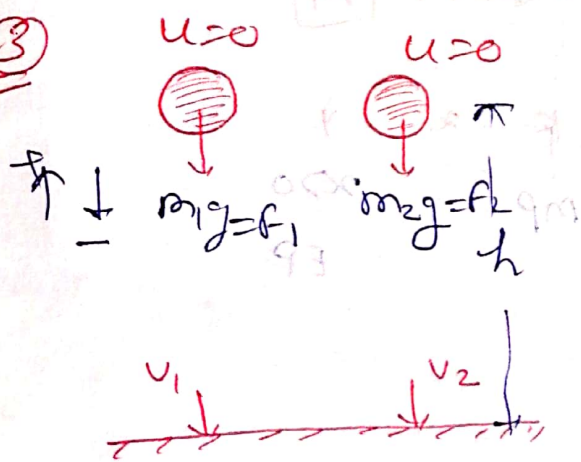
what is the force acting on it during its fall.

$$F = mg$$

$$= 1.5 \times 9.8$$

$$F = 14.7 \text{ N}$$

③



$$m_1 : m_2 = 1 : 2 \Rightarrow$$

a)  $v_1 : v_2 = ?$  when they strike the ground

b) force ratio during motion.

as  $v = u + at$   
 $v_1 = -gt$   
 $v_2 =$

a)  $v^2 = u^2 + 2gh$   
 $\therefore v_1^2 = \therefore 2gh$   
 $v_1 = \sqrt{2gh}$

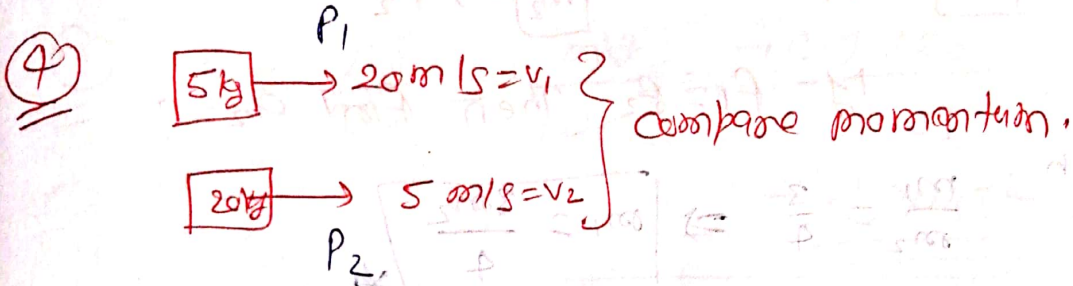


$$\frac{v_1}{v_2} = \frac{\sqrt{2gh}}{\sqrt{2gh}} = \underline{\underline{1:1}}$$

$$\textcircled{3} \frac{m_1}{m_2} = \frac{1}{2} \Rightarrow m_1 = \frac{m_2}{2}$$

$$\text{or } \boxed{m_2 = 2m_1}$$

$$\frac{F_1}{F_2} = \frac{m_1 g}{m_2 g} = \frac{m_1 g}{2m_1 g} = \underline{\underline{1:2}}$$



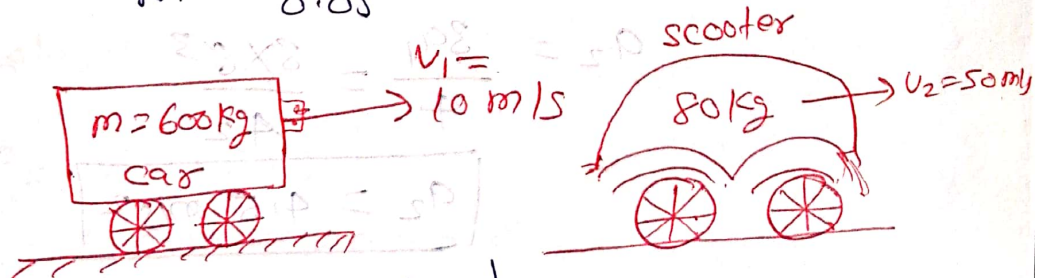
$$\frac{P_1}{P_2} = \frac{20 \times 5}{20 \times 5} = \underline{\underline{1:1}}$$

Q5 if mass  $m = 50 \text{ gm}$   $F = 20 \text{ N}$   
find  $a = ?$

$$m = 50 \text{ gm} = 0.05 \text{ kg}$$

$$a = \frac{F}{m} = \frac{20}{0.05} = 400 \text{ m/s}^2$$

Q6



a)  $P_1 : P_2$

$$\frac{P_1}{P_2} = \frac{600 \times 10}{80 \times 50}$$

$$\boxed{P_1/P_2 = 3/2}$$

i)  $P_1 = mv$   
 $= 600 \times 10 = 6000$

$P_2 = 80 \times 50 = 4000$

$\boxed{P_1 > P_2}$  car required more force.

b) which vehicle require more force to stop  
1) same interval (1) same dist.

ii)  $\boxed{v_1 < v_2}$

so scooter required more force.

7

$10 \text{ kg} \rightarrow 2 \text{ kgf} = F$   
 $F = 2 \times 9.8 \text{ N}$   
 $F = 19.6 \text{ N}$

$a_2 = ?$

$$a = \frac{F}{m} = \frac{19.6}{10} = 1.96 \text{ m/s}^2$$

8

$$m_1 : m_2 = 3 : 4$$

$$\rightarrow a_1 = 6 \text{ m/s}^2$$

$$\rightarrow a_2 = ?$$

$$m_1 \rightarrow F_1$$

$$m_2 \rightarrow F_2$$

If  $F_1 = F_2$  Then find  $a_2 = ?$

Sol<sup>n</sup>

$$\frac{m_1}{m_2} = \frac{3}{4} \Rightarrow$$

$$m_1 = \frac{3m_2}{4}$$

$$\therefore a = \frac{F}{m}$$

$$\therefore \frac{a_1}{a_2} = \frac{F_1/m_1}{F_2/m_2} = \frac{F/3m_2/4}{F/m_2}$$

$$= \frac{4F}{3m_2} \times \frac{m_2}{F}$$

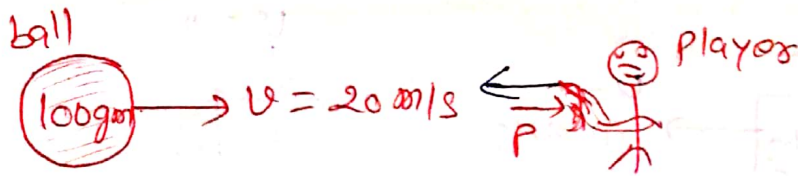
$$\frac{a_1}{a_2} = \frac{4}{3}$$

$$a_2 = \frac{3a_1}{4} = \frac{3 \times 6}{4}$$

$$a_2 = 4.5 \text{ m/s}^2$$



9



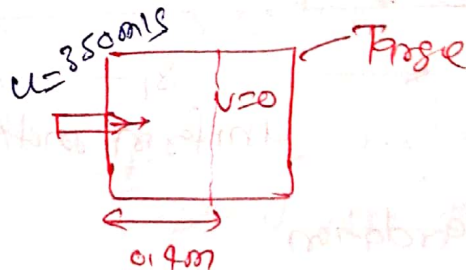
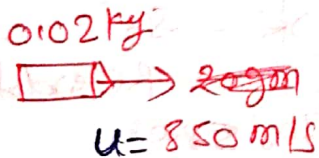
i) ball strikes player hand and comes rest in 0.01 sec  
find force applied by the ball on player hand

ii)  $a_{\text{ball}} = ?$

i  $F = \frac{\Delta p}{\Delta t} = \frac{mv}{\Delta t} = \frac{-0.1 \times 20}{0.01}$   
 $= -2 \times 10^2$   
 $F = -200 \text{ N}$

ii  $a = \frac{F}{m} = \frac{-200}{0.1} = -2000 \text{ m/s}^2$

10



i) find force = ?

ii) Retardation?

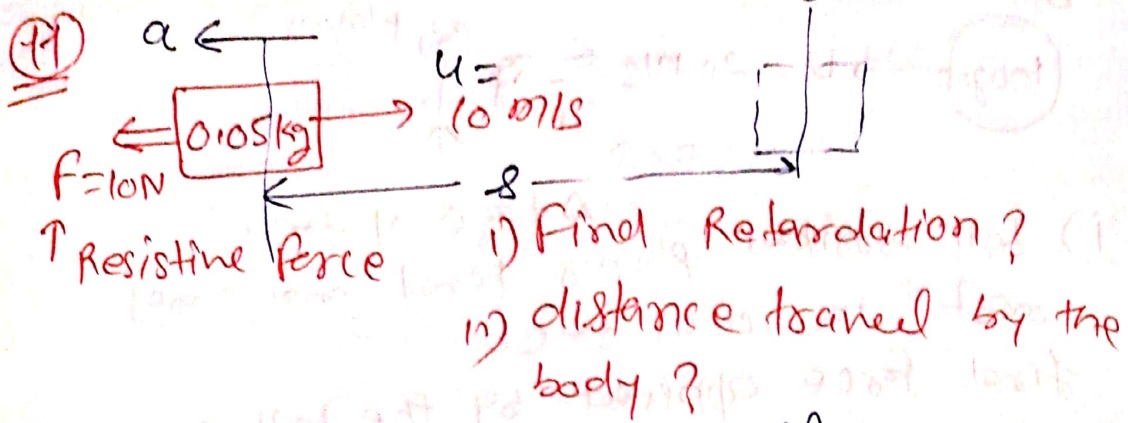
$v^2 = u^2 + 2as$

$0 = (350)^2 + 2a \times 0.4$

$a = -\frac{350 \times 350}{2 \times 4 \times 10^{-1}} = -1.53 \times 10^5 \text{ m/s}^2$

iii) force applied by the bullet  $F = ma$

$F = 0.02 \times 1.53 \times 10^5$   
 $F = 3062.5 \text{ N}$



$$F = -ma$$

$$10 = -0.05 \times a$$

$$a = \frac{-10}{0.05} = -200 \text{ m/s}^2$$

$$\boxed{a = -200 \text{ m/s}^2}$$

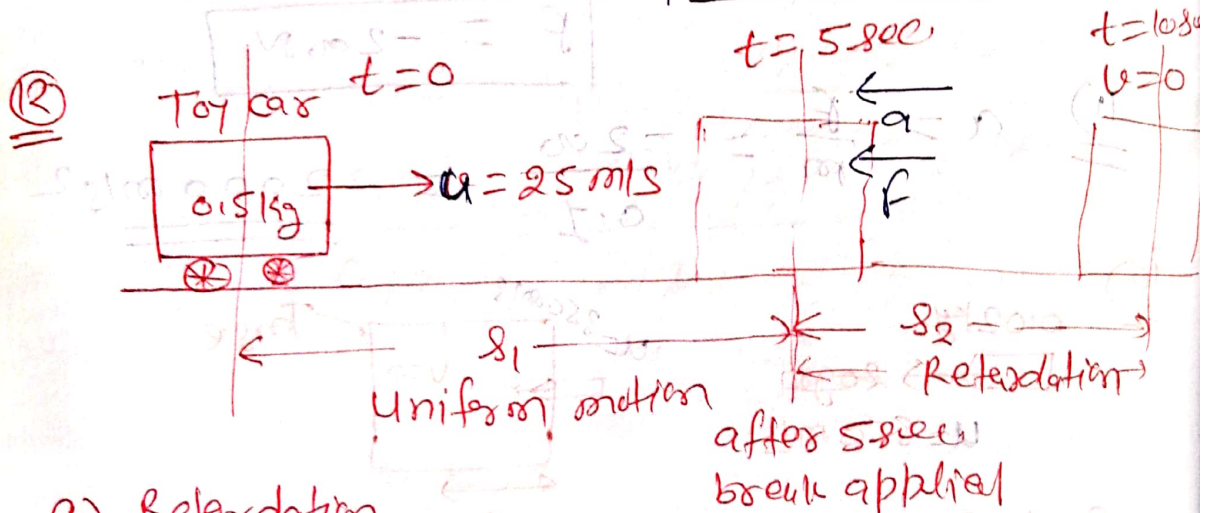
$$v^2 = u^2 + 2as$$

$$0 = 10^2 - 2 \times 200 \times s$$

$$100 = 400s$$

$$s = 0.25 \text{ m}$$

$$\boxed{s = 25 \text{ cm}}$$



- Retardation
- $s_2 = ?$  (distance after brakes)
- force exerted by the brakes?

a

$$v = u + at$$

$$0 = 25 + a \times 5.8$$

$$\boxed{a = -2.5 \text{ m/s}^2}$$

$$-625 = -5s_2$$

$$\boxed{s_2 = 125 \text{ m}}$$

b

$$v^2 = u^2 + 2as$$

$$0 = (25)^2 - 2 \times 2.5 \times s_2$$

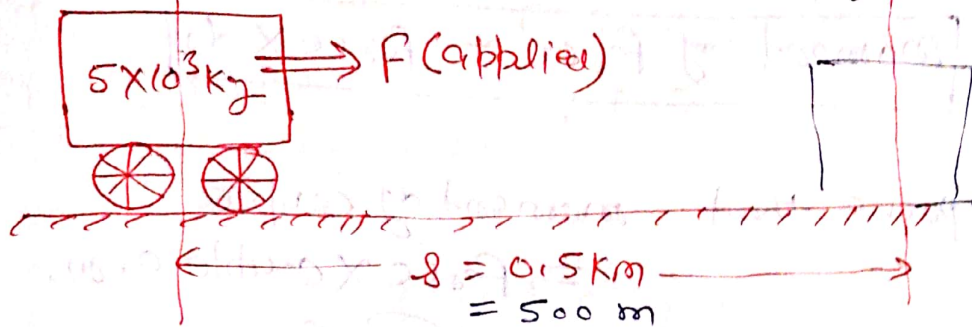
$$\boxed{F = -1.25 \text{ N}}$$



13

Rest

Truck  $u=0$



A force  $F$  is applied and truck travel  $0.5 \text{ km}$  in  $10 \text{ sec}$ .

find  $a = ?$  &  $F = ?$

Soln  $s = ut + \frac{1}{2} at^2$

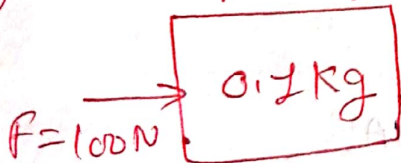
$$0.5 \times 10^3 = \frac{1}{2} a \times 100 \text{ so}$$

$$a = \frac{8 \times 10^1}{500/100} \Rightarrow \boxed{a = 10 \text{ ms}^{-2}}$$

(b)  $F = ma$   
 $= 5 \times 10^3 \times 10 = 5 \times 10^4 \text{ N}$

14

Rest  $u=0$



for  $0.1 \text{ s}$

A force  $100 \text{ N}$  is applied on the body for  $0.1 \text{ sec}$ .

- a)  $p = ?$
- b) distance traveled in  $0.1 \text{ sec}$ . Take  $g = 10 \text{ ms}^{-2}$

i)  $F = \frac{\Delta p}{\Delta t}$

$$\Delta p = F \Delta t$$
$$= 100 \times 0.1$$

$$\boxed{\Delta p = 10 \text{ N}\cdot\text{s}}$$

ii)

$$F = ma$$

$$a = \frac{100}{0.2} = 1000 \text{ ms}^{-2}$$

$$s = ut + \frac{1}{2} at^2$$

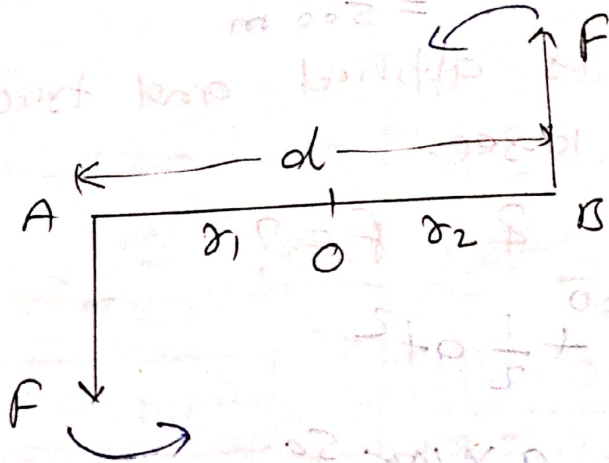
$$= 0 + \frac{1}{2} \times 1000 \times (10^{-1})^2$$

$$\boxed{s = 5 \text{ m}} \quad \underline{\underline{\text{Ans}}}$$

## Exercise 1(B)

① moment of force = force  $\times$   $d_{\perp}$

② prove that moment of couple = force  $\times$  couple arm.



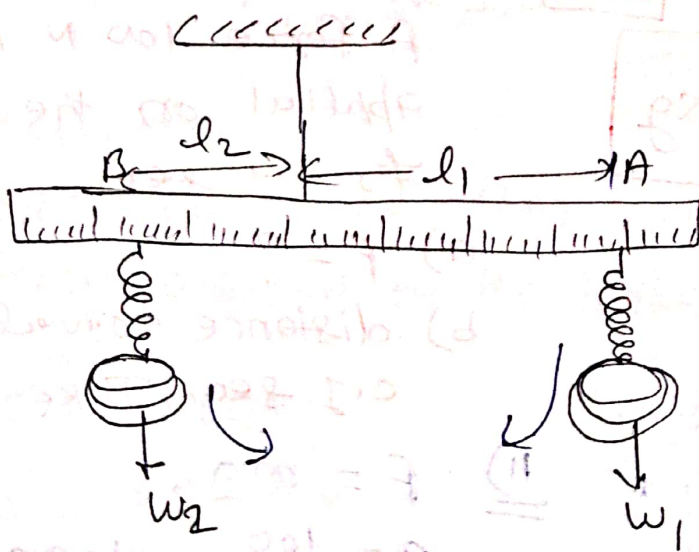
moment of couple =  $F \times r_1 + F \times r_2$   
(T)

=  $F(r_1 + r_2)$

=  $Fd$

↑ ↑  
Force    couple arm

⑧



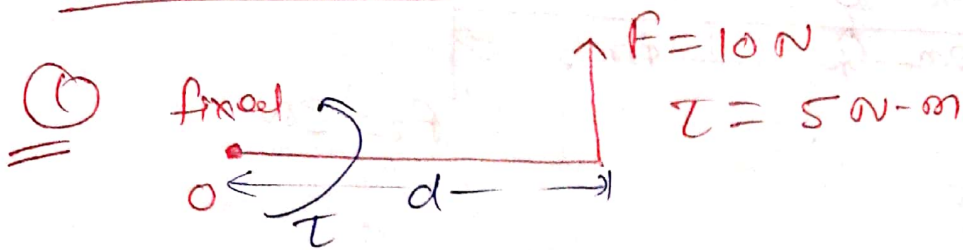
for equilibrium,

$w_1 l_1 = w_2 l_2$

principle of moments.



# Numericals 12

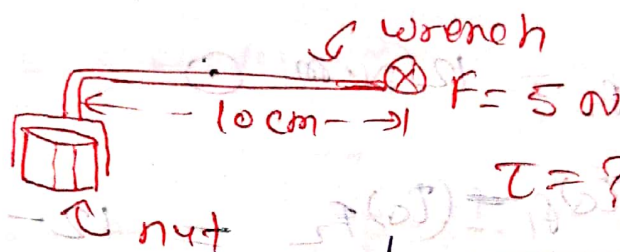


$$\tau = F \cdot d$$

$$5 = 10 \cdot d$$

$$d = \frac{5}{10} = \underline{\underline{0.5 \text{ m}}}$$

Q2



$$\tau = ?$$

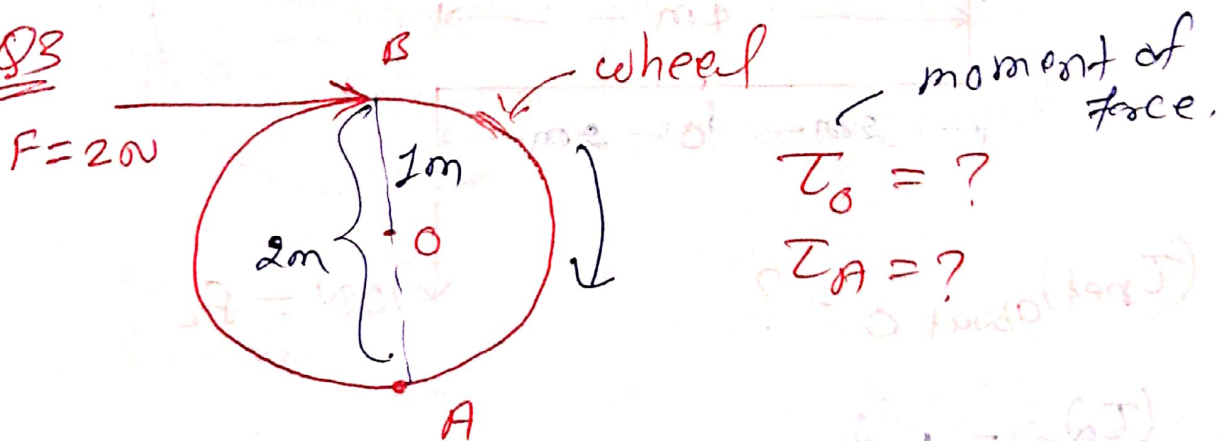
$$d = 10 \text{ cm} = \underline{\underline{0.1 \text{ m}}}$$

$$\tau = F \cdot d$$

$$= 5 \times 0.1$$

$$\boxed{\tau = 0.5 \text{ N}\cdot\text{m}}$$

Q3



$$\tau_O = ?$$

$$\tau_A = ?$$

$$\tau_O = 2 \times 1$$

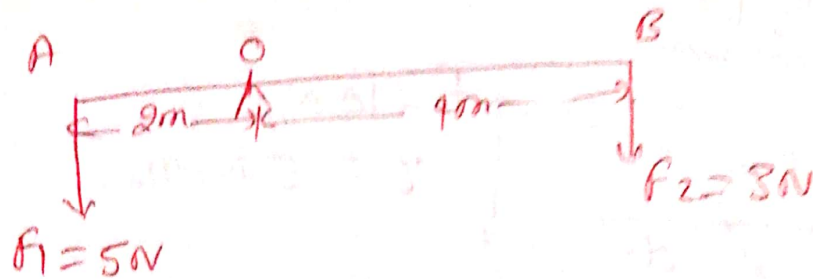
$$= \underline{\underline{2 \text{ N}\cdot\text{m}}}$$

$$\tau_A = F \times AB$$

$$= 2 \times 2$$

$$\boxed{\tau_A = 4 \text{ N}\cdot\text{m}}$$

Q.4



- a) moment of force  $f_1$  about O  
b) ——— ———  $f_2$  ———  
c) Total moment = ?

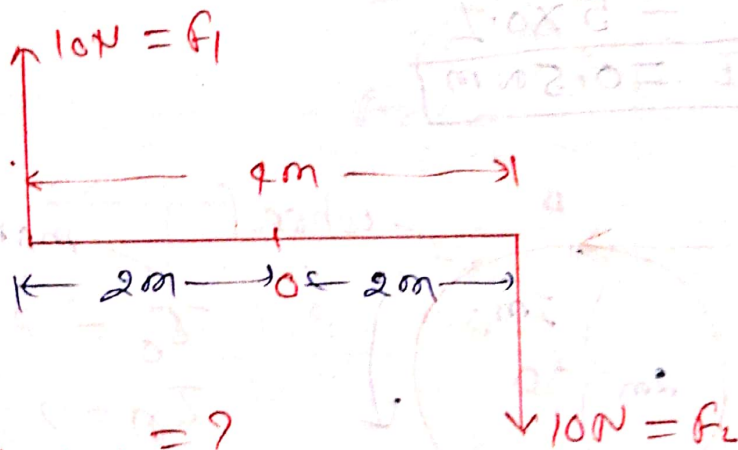
$$\underline{f_1} \quad (\tau_o)_{f_1} = 10 \text{ N}\cdot\text{m} \quad \otimes$$

$$\underline{f_2} \quad (\tau_o)_{f_2} = 12 \text{ N}\cdot\text{m} \quad \odot$$

$$\tau = (\tau_o)_{f_1} + (\tau_o)_{f_2} = 12 - 10$$

$$\boxed{\tau = \cancel{22 \text{ N}\cdot\text{m}}} = \underline{2 \text{ N}\cdot\text{m}} \quad \odot$$

Q.5



$(\tau_{\text{net}})_{\text{about O}} = ?$

$$(\tau_o)_{f_1} = 10 \times 2 = 20 \text{ N}\cdot\text{m} \quad \otimes$$

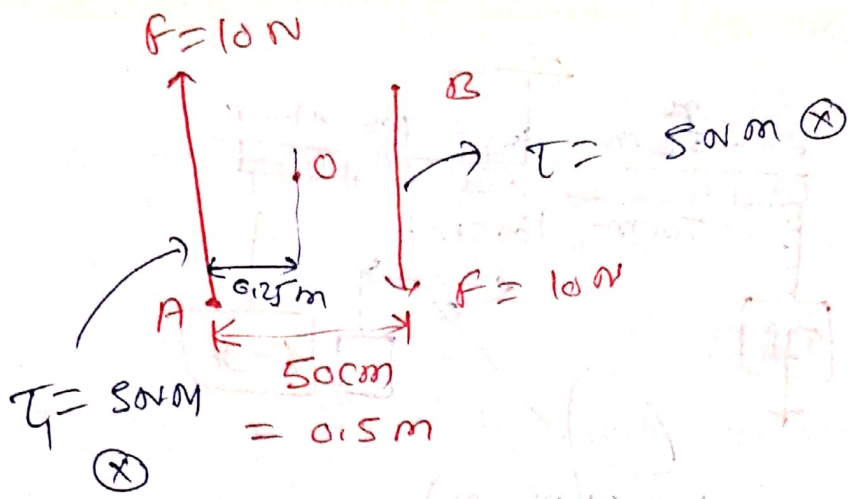
$$(\tau_o)_{f_2} = 20 \text{ N}\cdot\text{m} \quad \otimes$$

$$\tau_{\text{net}} = 20 + 20$$

$$= 40 \text{ N}\cdot\text{m} \quad \otimes$$

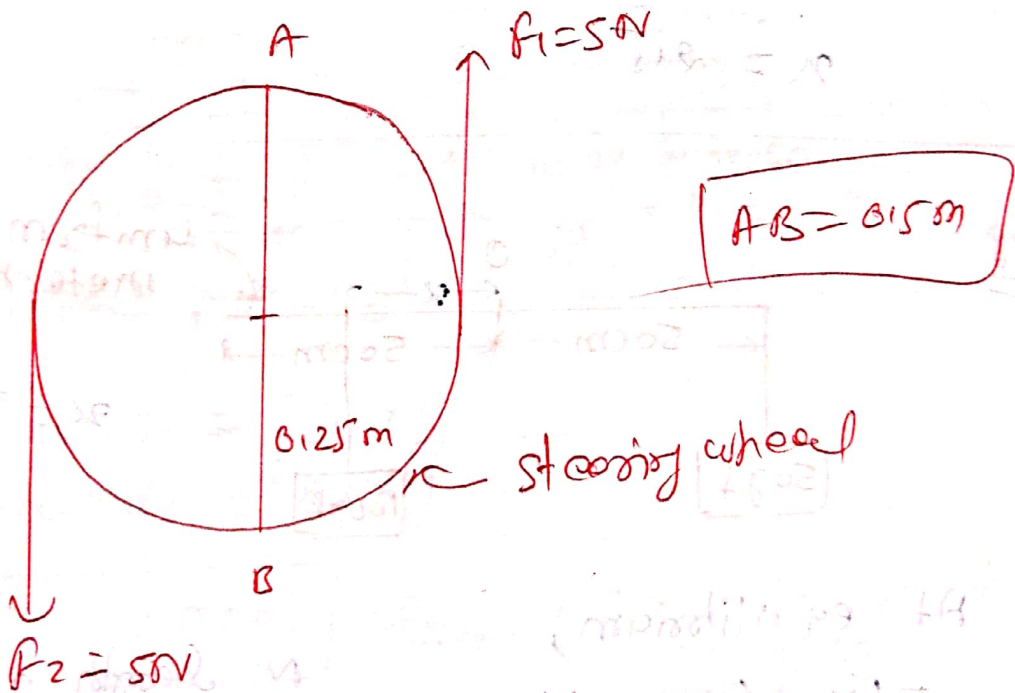


Q6



$$\begin{aligned}(\tau_{\text{net}})_O &= 10 \times 0.125 + 10 \times 0.125 \\ &= 2.5 + 2.5 \\ &= 5\text{ N-m}\end{aligned}$$

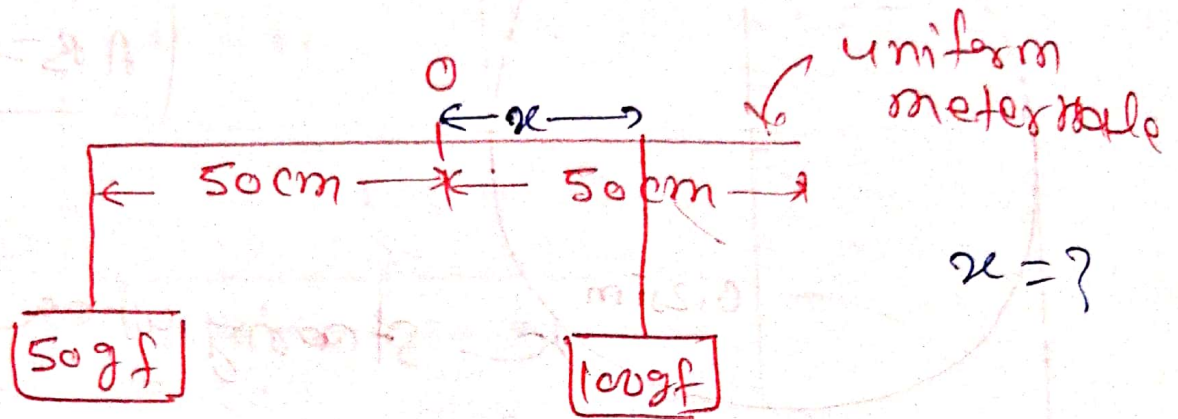
Q7



moment of couple = either, force  $\times$  couple arm

$$\begin{aligned}&= 5 \times 0.5 \\ &= \underline{\underline{2.5\text{ Nm}}}\end{aligned}$$

Q8



At equilibrium,

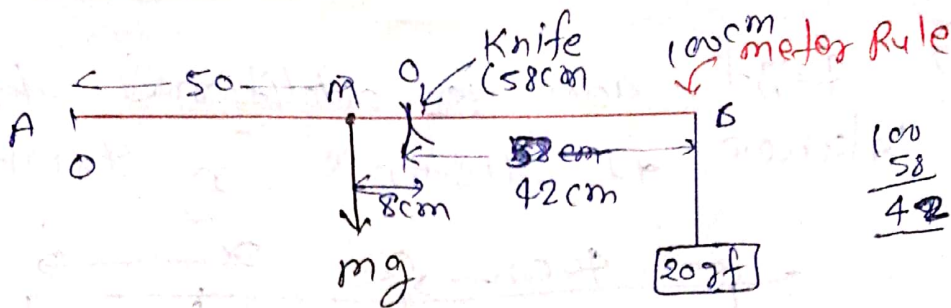
$$50 \cancel{\phi} \times 50 = 100 \cancel{\phi} \times x$$

$$\boxed{x = 25 \text{ cm}}$$

N. Length of  
meter rule  
= 100 cm



Q9



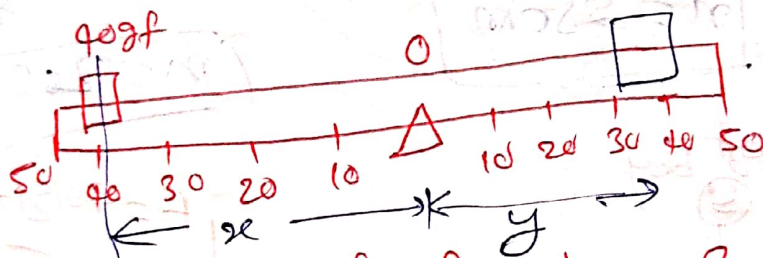
mg of meter scale work at its mid point.

$$mg \times 8 = 20 \times 42$$

$$w = \frac{20 \times 42}{8}$$

$$w = 105 \text{ gf}$$

Q10



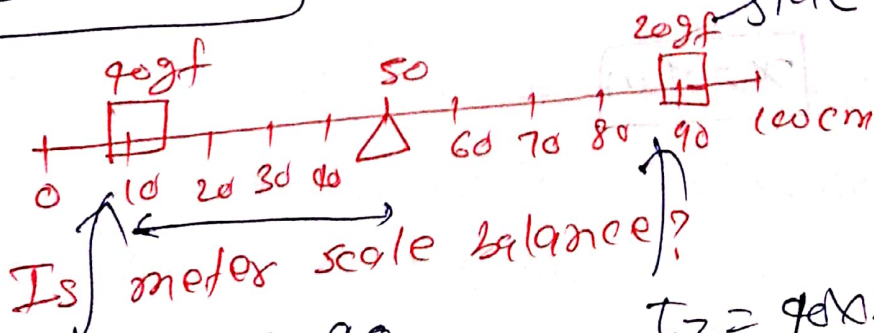
where put 80 gf by balance?

$$40 \times x = 80 \times y$$

$$20 \times x = 80 \times y$$

$$y = 20 \text{ cm}$$
 from point O to right side

Q11

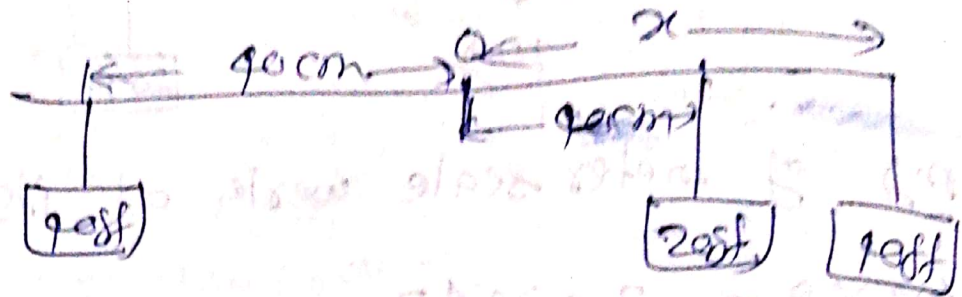


$$\tau_1 = 90 \times 10 = 1600 \text{ Nm}$$

$$\tau_2 = 20 \times 90 = 1800 \text{ Nm}$$

$$\tau_1 \neq \tau_2$$

11) 90gf add for additional for balance, at distance  $x$  from 90gf



$$90 \times 40 = \cancel{20 \times 40} + 90 \times x$$

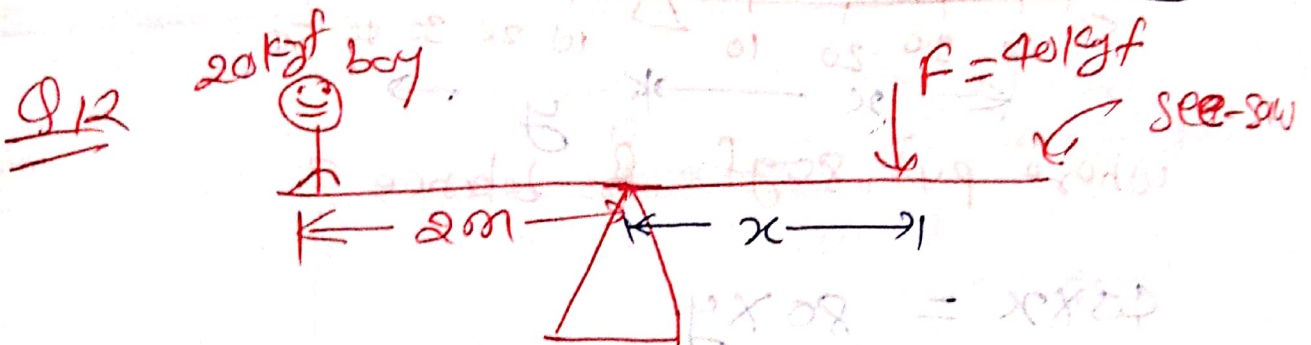
$$1600 = 800 + 90x$$

$$\cancel{90x = 1600}$$

$$x = 25 \text{ cm}$$

$$x = \frac{20}{90}$$

$$x = 20 \text{ cm}$$



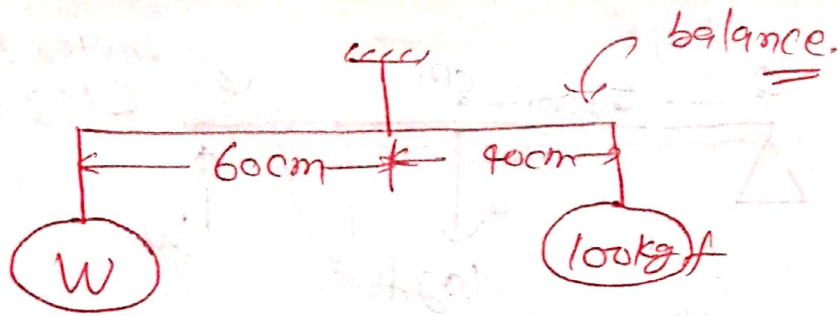
for balancing condition,

$$\cancel{20 \times 2} = x \times \cancel{40}$$

$$x = 1 \text{ m}$$



Q13

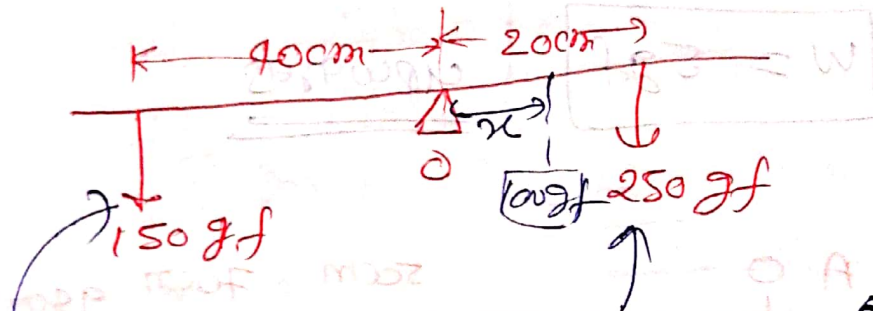


$$W \times 60 = 40 \times 100$$

$$W = \frac{4000}{60} = 66.66$$

$$W = 66.66 \text{ kgf}$$

Q14



$$\tau_1 = 150 \times 40$$

$$\tau_1 = 6000 \text{ Nm}$$

⊙ anti

$$\tau_2 = 250 \times 20$$

$$\tau_2 = 5000 \text{ Nm}$$

⊗ clockwise

$$\tau_1 - \tau_2 = \frac{6000}{-5000}$$

$$\frac{1000}{\ominus} \text{ Anticlockwise}$$

\* Let 100gf placed at distance  $x$ ,

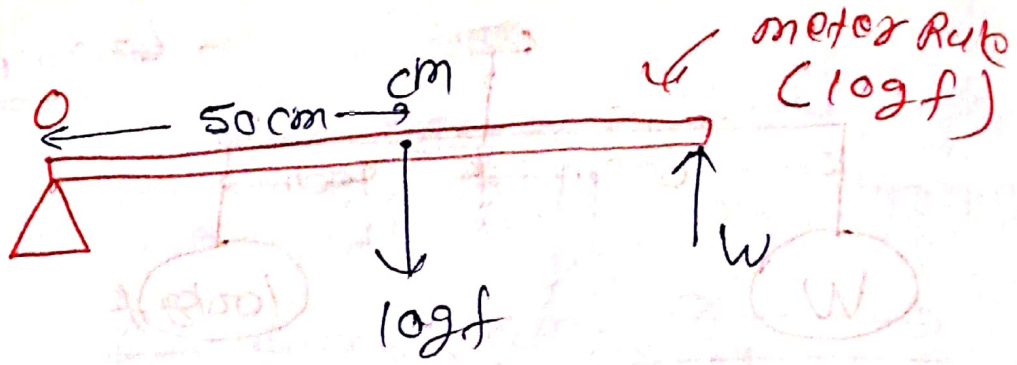
Then  $150 \times 40 = 100 \times x + 250 \times 20$

$$60 = x + 50$$

$$x = 60 - 50$$

$$x = 10 \text{ cm}$$

Q15



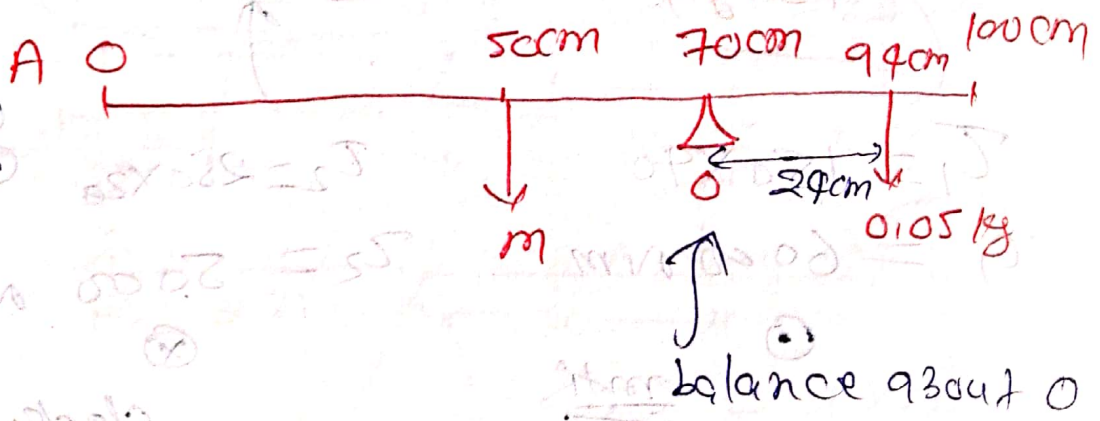
$$\tau = 10 \times 50$$
$$\tau = 500 \text{ gf cm}$$

for equilibrium,

$$10 \times 50 = W \times 100$$

$$W = 5 \text{ gf} \quad \underline{\underline{\text{upwards}}}$$

Q16



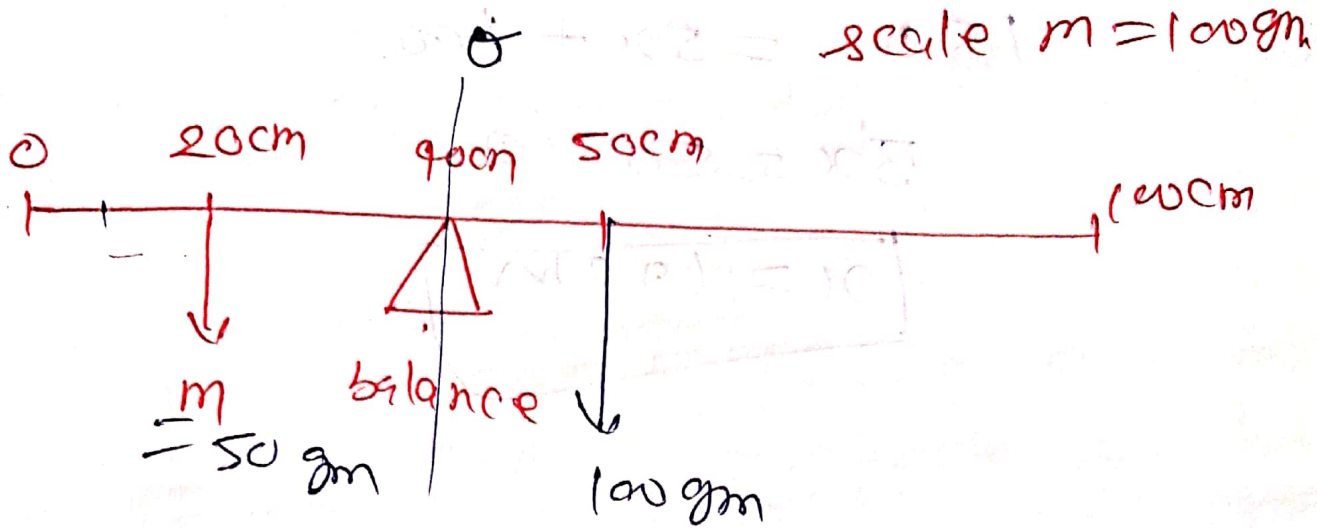
by equilibrium condition,

$$m \times 20 = 0.05 \times 24$$

$$m = \frac{0.05 \times 24}{20}$$

$$m = 0.06 \text{ kg}$$

Q17



moment about 0,

$$m \times 20 = 100 \times 10$$

$$m = 50 \text{ gm}$$

\* when  $m$  moved to 10cm mark.

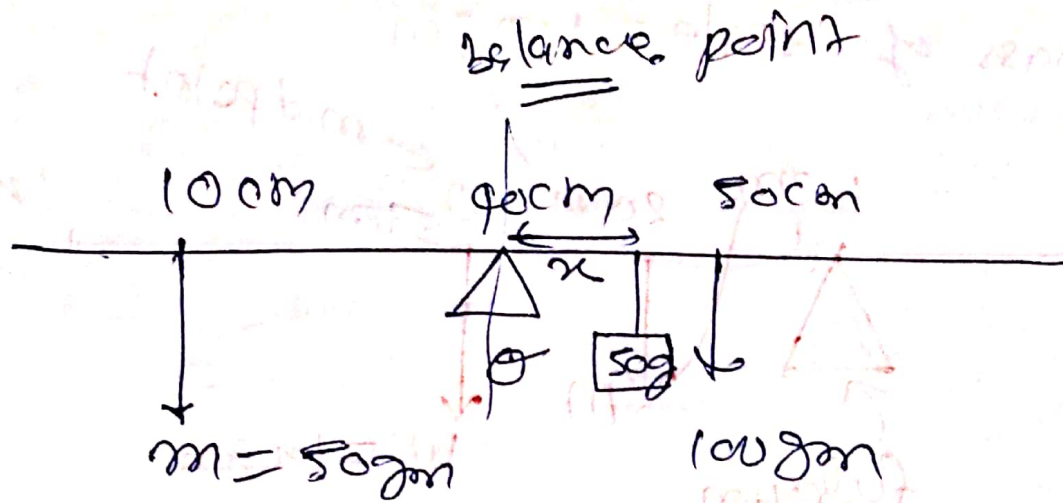
$$\tau_{\text{net}} = 100 \times 10 + 50 \times 30$$

⊗                      ⊙

$$= -1000 + ~~1000~~ 1500$$

$$\tau_{\text{net}} = \underline{\underline{500 \text{ gm}}}$$





$$50 \times 30 = 50 \times x + 100 \times 10$$

$$1500 = 50x + 1000$$

$$- 50x = 500$$

$$x = 10 \text{ cm}$$